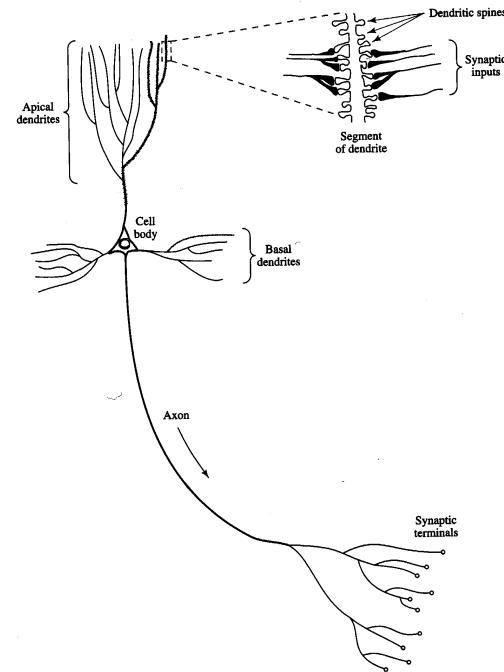
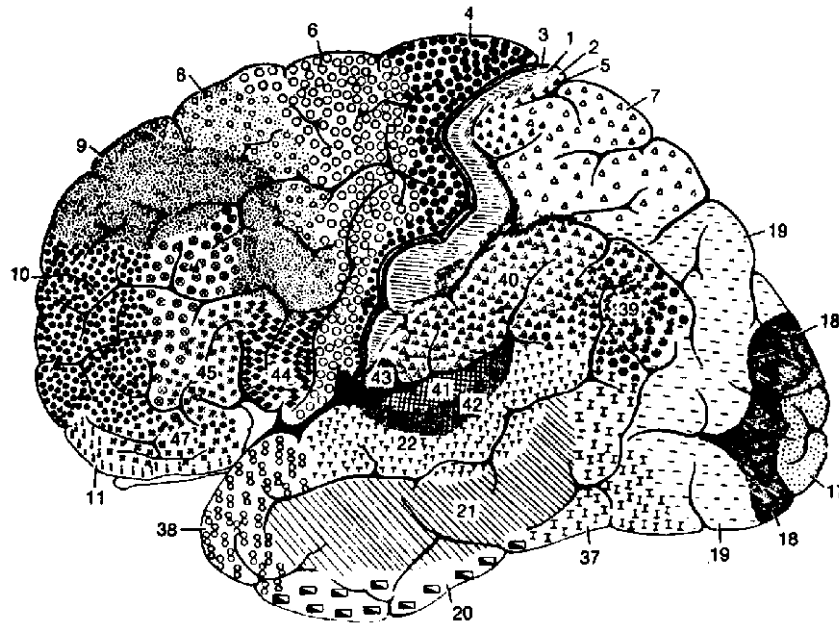


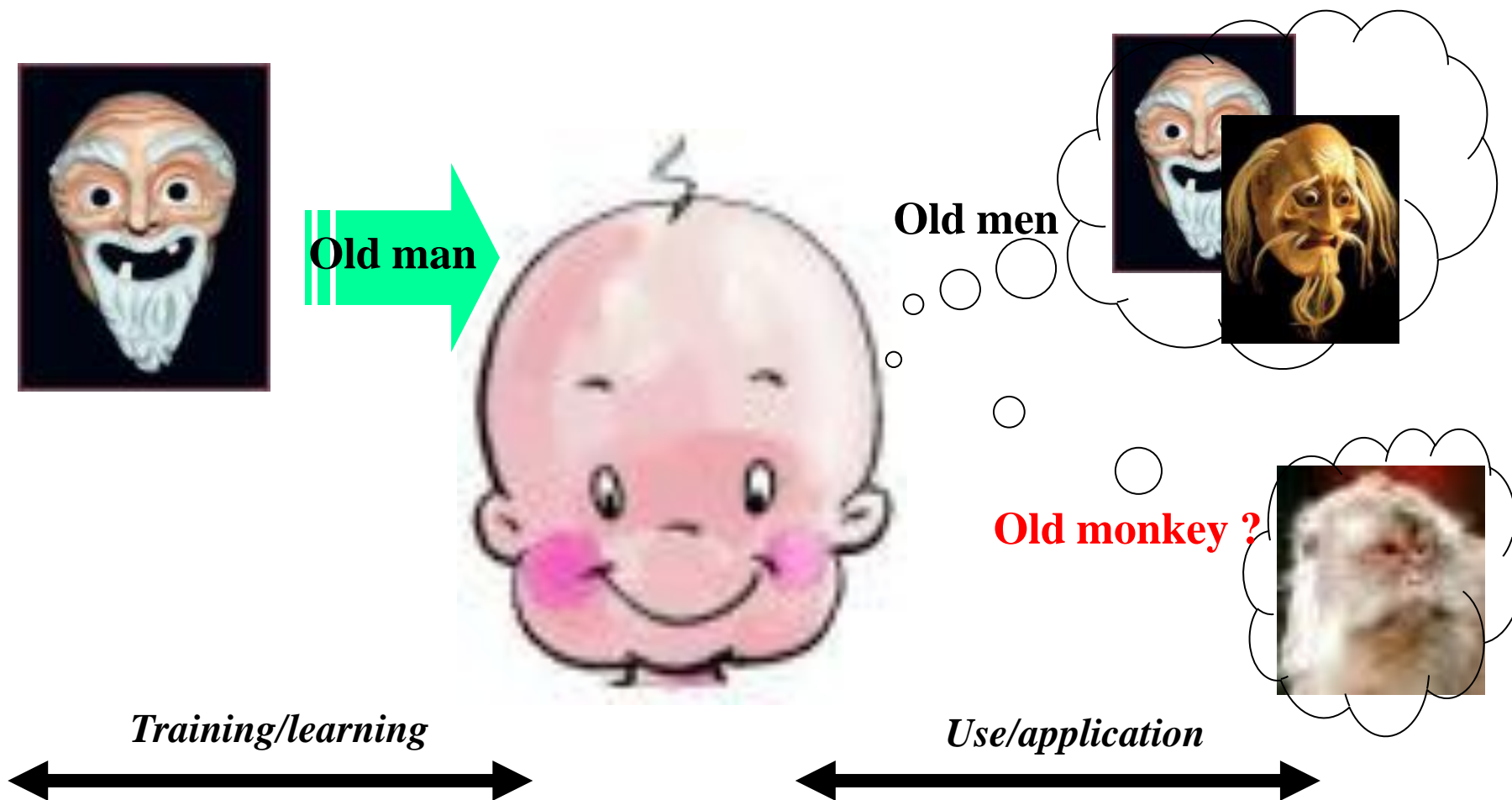
# ***Neural Networks and Gas Turbine Diagnostics***

# Artificial Neural Networks

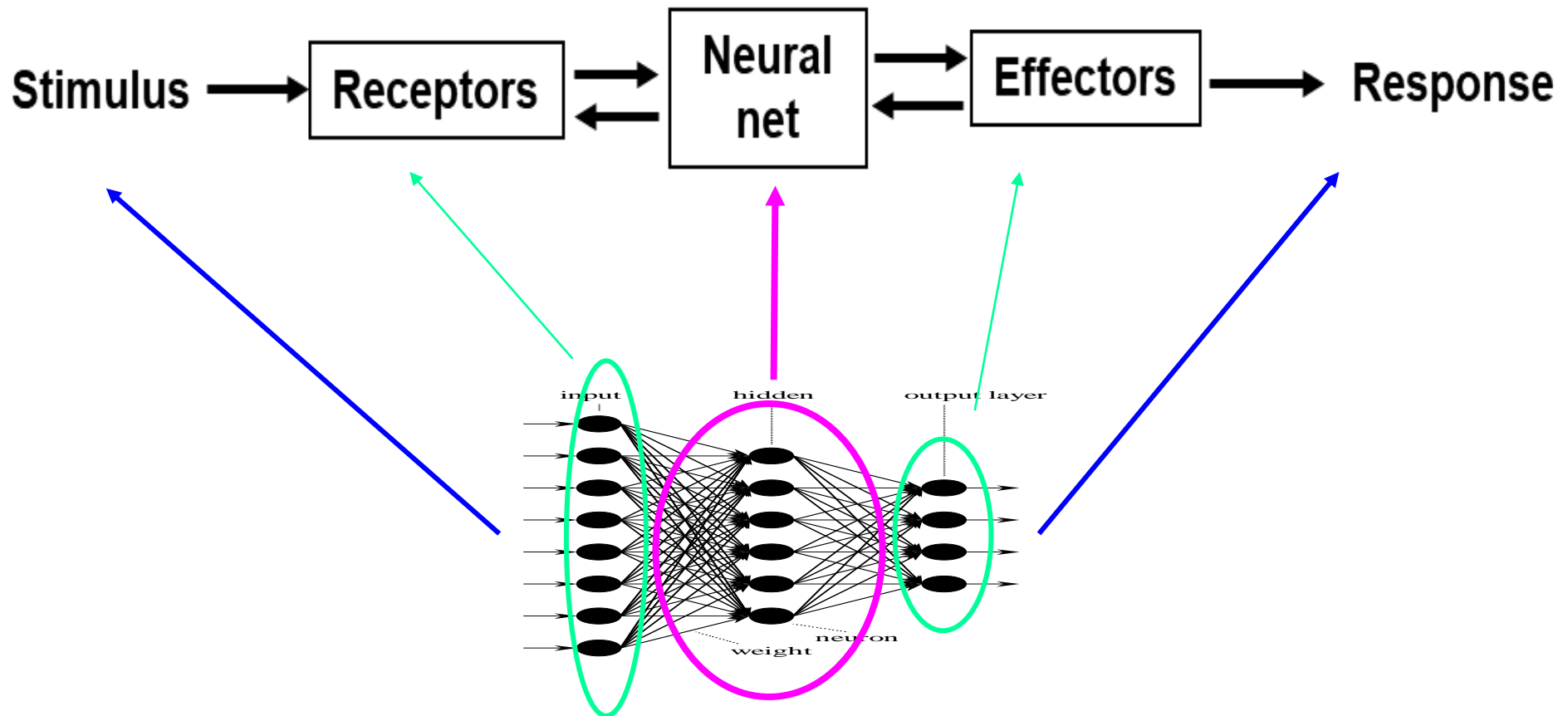


- Work on ANN has been motivated by the recognition that the human brain computes entirely differently from computers
- A brain learns from experience

# Artificial Neural Networks



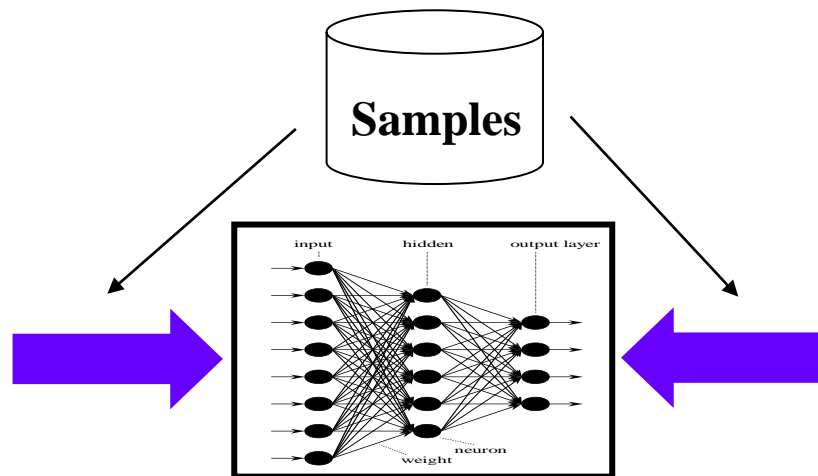
# Artificial Neural Networks



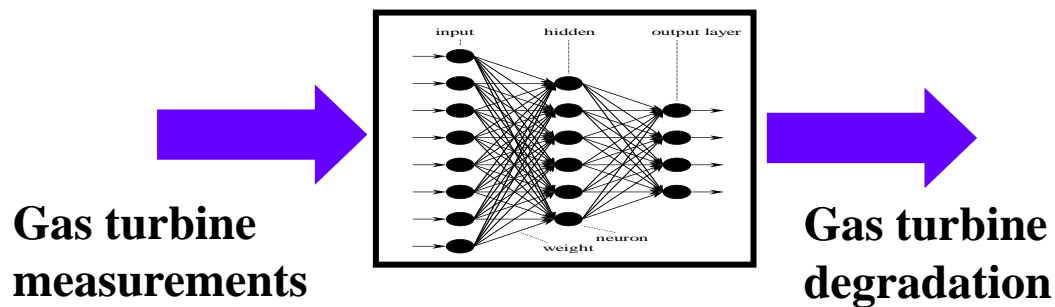
**Neural network:** a massively parallel distributed processor made up of simple processing units, which has a natural propensity for storing experimental knowledge and making it available for use.

# Artificial Neural Networks

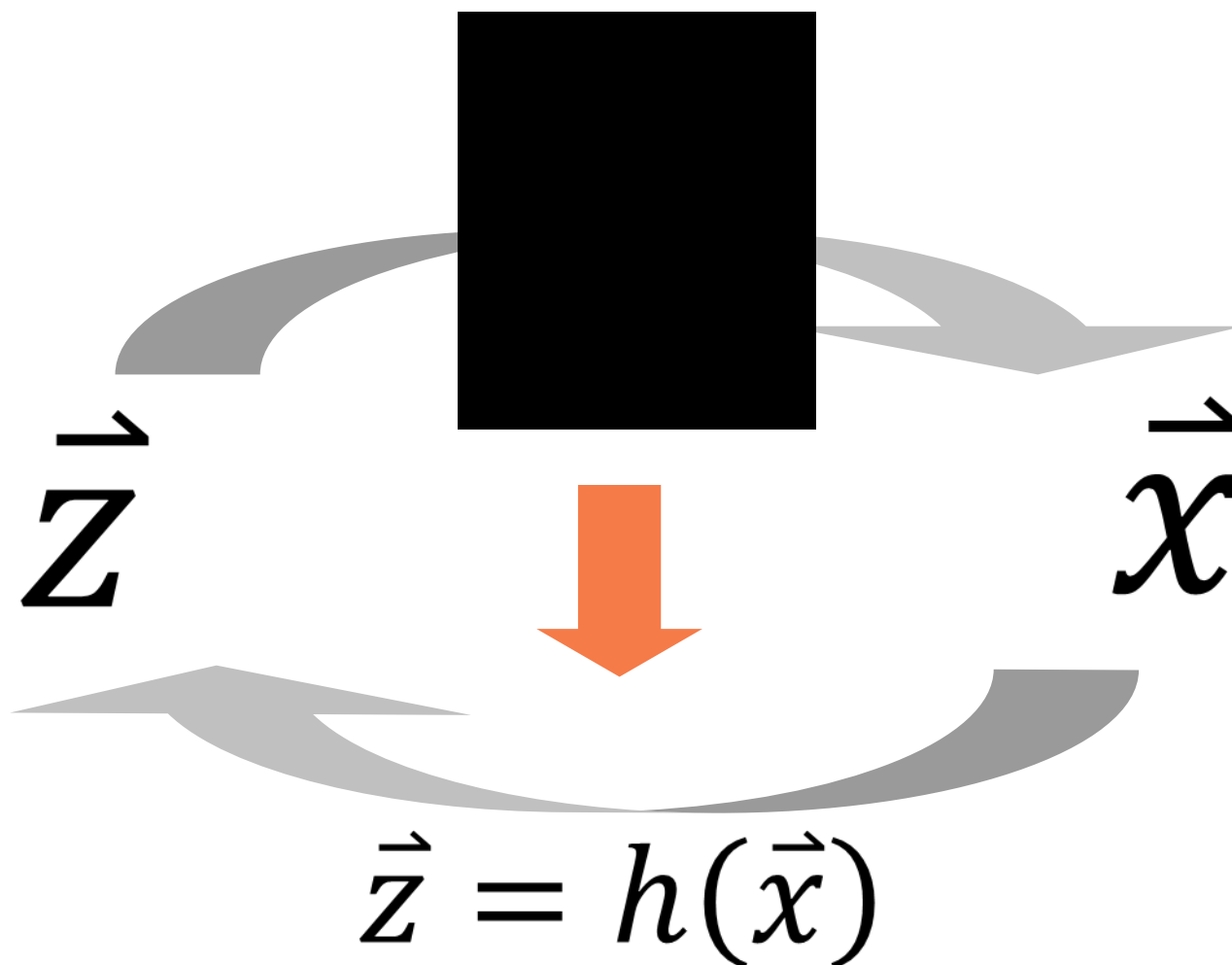
## Training of ANN:



## Application of ANN:

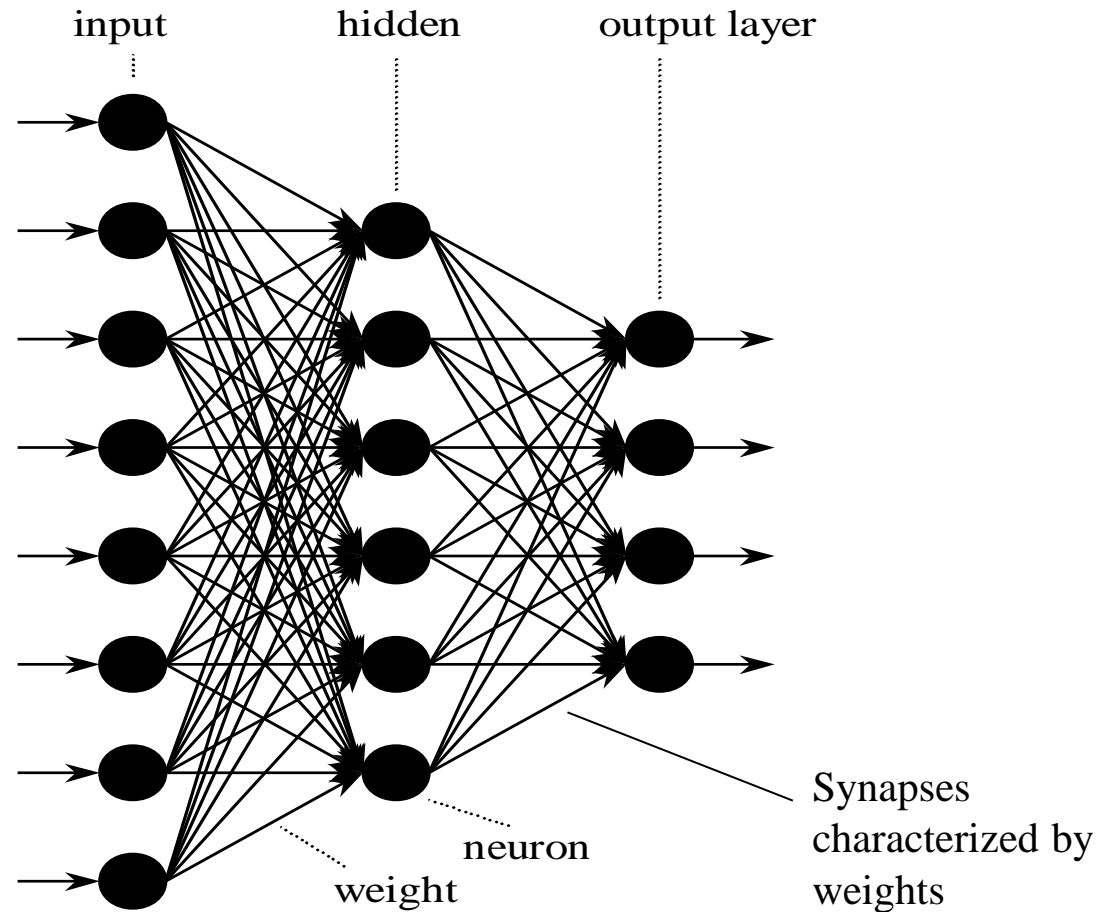


# Artificial Neural Networks



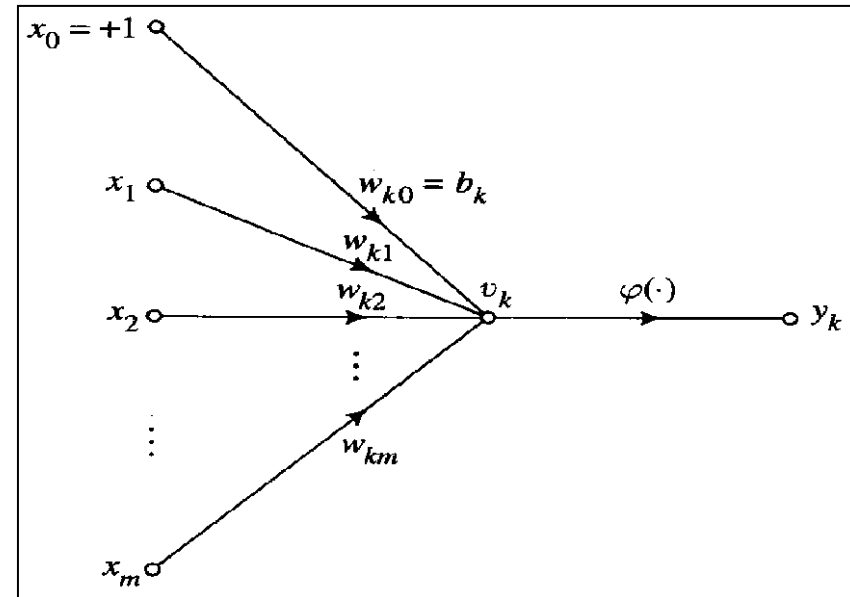
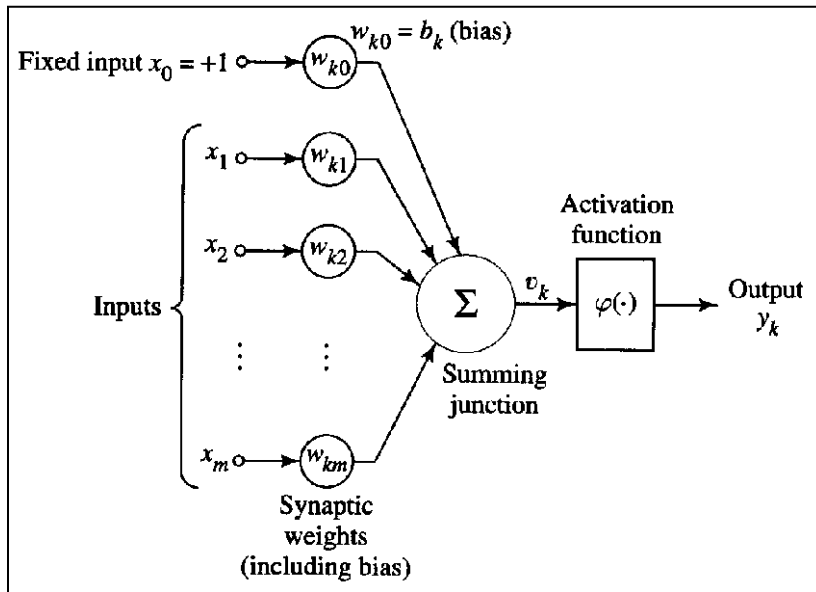
# Artificial Neural Networks

## A typical Neural Network



# Artificial Neural Networks

A neuron is an information-processing unit – fundamental to the operation of NN



## THREE KEY ELEMENTS:

- ✓ A set of synapses
- ✓ An adder
- ✓ An activation function

Signal-flow graph of a neuron

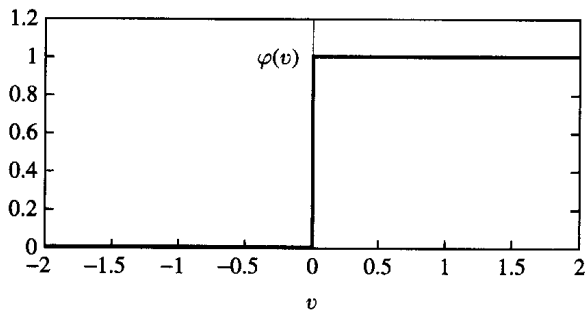
$$y_k = \varphi \left( \sum_{j=1}^m w_{kj} x_j + b_k \right)$$



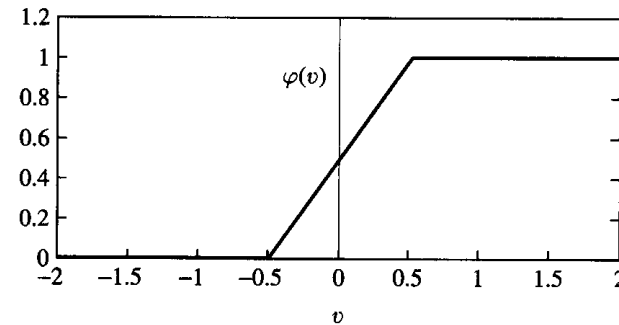
# Artificial Neural Networks

## Activation function to take into account non-linearity:

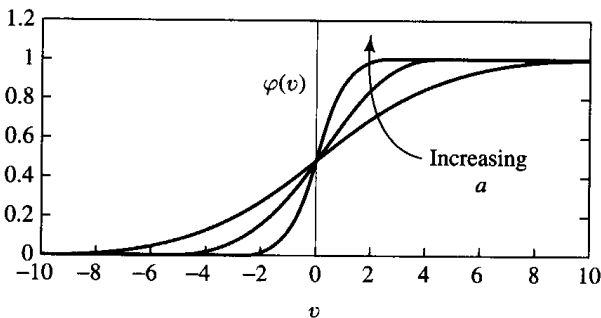
*Threshold Function:*



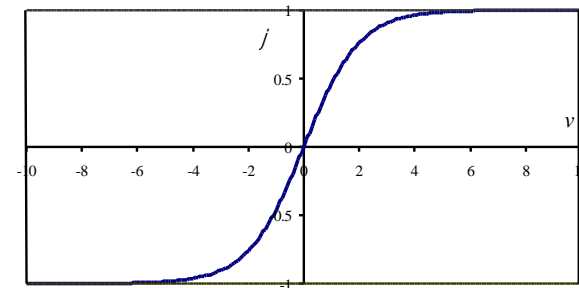
*Piecewise-Linear Function:*



*Sigmoid function (logistic function):*  $\varphi(v) = \frac{1}{1 + \exp(-av)}$



*Sigmoid function (hyperbolic tangent function):*  $\varphi(v) = \tanh(v) = \frac{1 - e^{-v}}{1 + e^{-v}}$



# Artificial Neural Networks

Samples: Examples of individual cases – experience:

$$\begin{pmatrix} \vec{z}_1 & \vec{x}_1 \\ \vec{z}_2 & \vec{x}_2 \\ \dots & \dots \\ \vec{z}_3 & \vec{x}_3 \end{pmatrix}$$

• Training samples

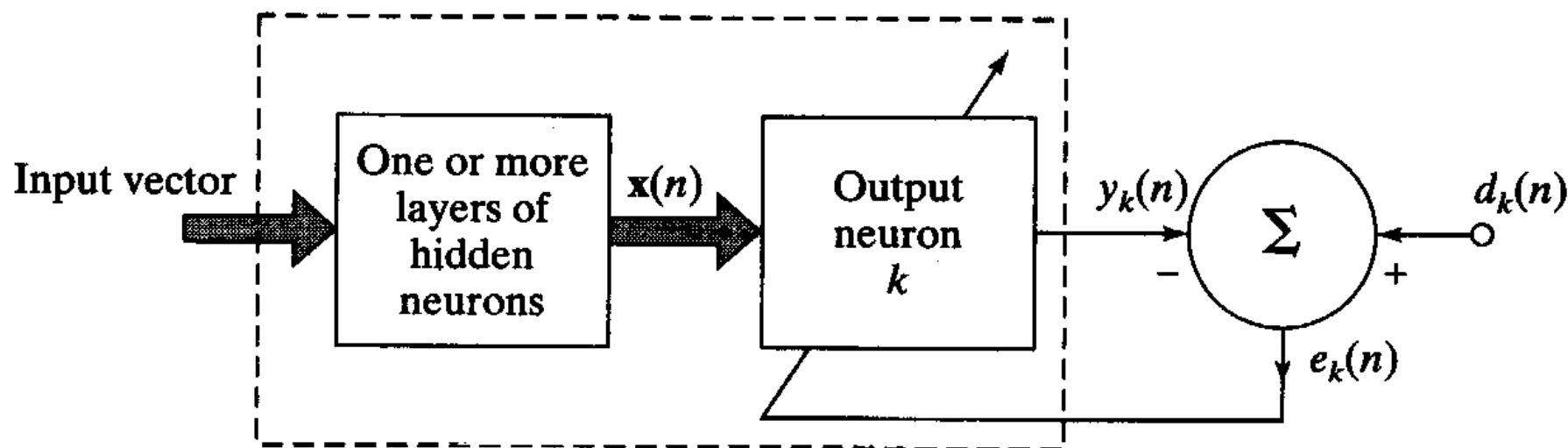
• Validation/Test samples

Observable  
information

Truth

# Artificial Neural Networks

## Training Algorithm: Feed-Forward Back-Propagation (FFBP)



# Artificial Neural Networks

## Rate of learning:

$$w_{ji}(n) = w_{ji}(n-1) + \Delta w_{ji}(n)$$

$$\Delta w_{ji}(n) = -\eta \frac{\partial E(n)}{\partial w_{ji}(n)} + \alpha \Delta w_{ji}(n-1)$$

where  $E(n) = \frac{1}{2} \sum_{j=1}^p e_j^2(n)$        $e_j(n) = d_j(n) - y_j(n)$

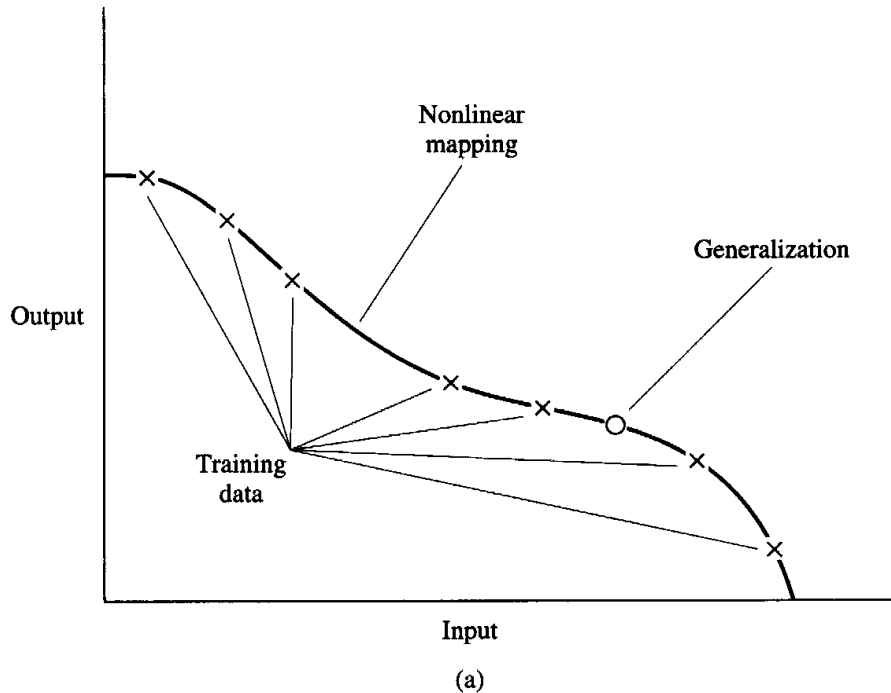
$\eta$  -- learning rate parameter       $\alpha$  -- constant

A low  $\eta$  produces slow training process;

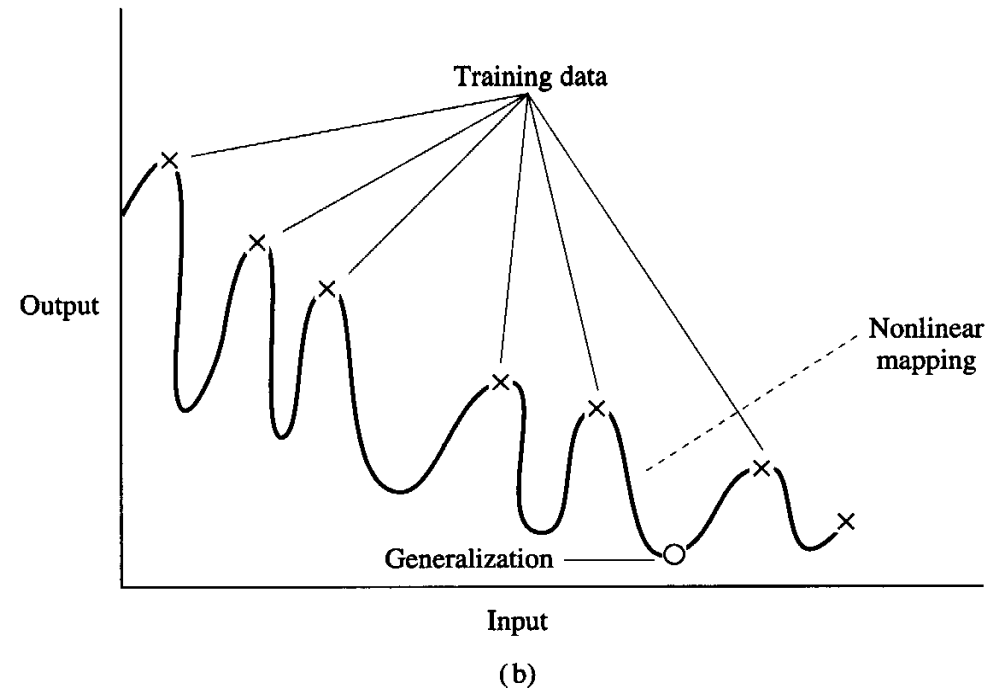
A large  $\eta$  may introduce instability to the learning curve

# Artificial Neural Networks

## Training Quality:



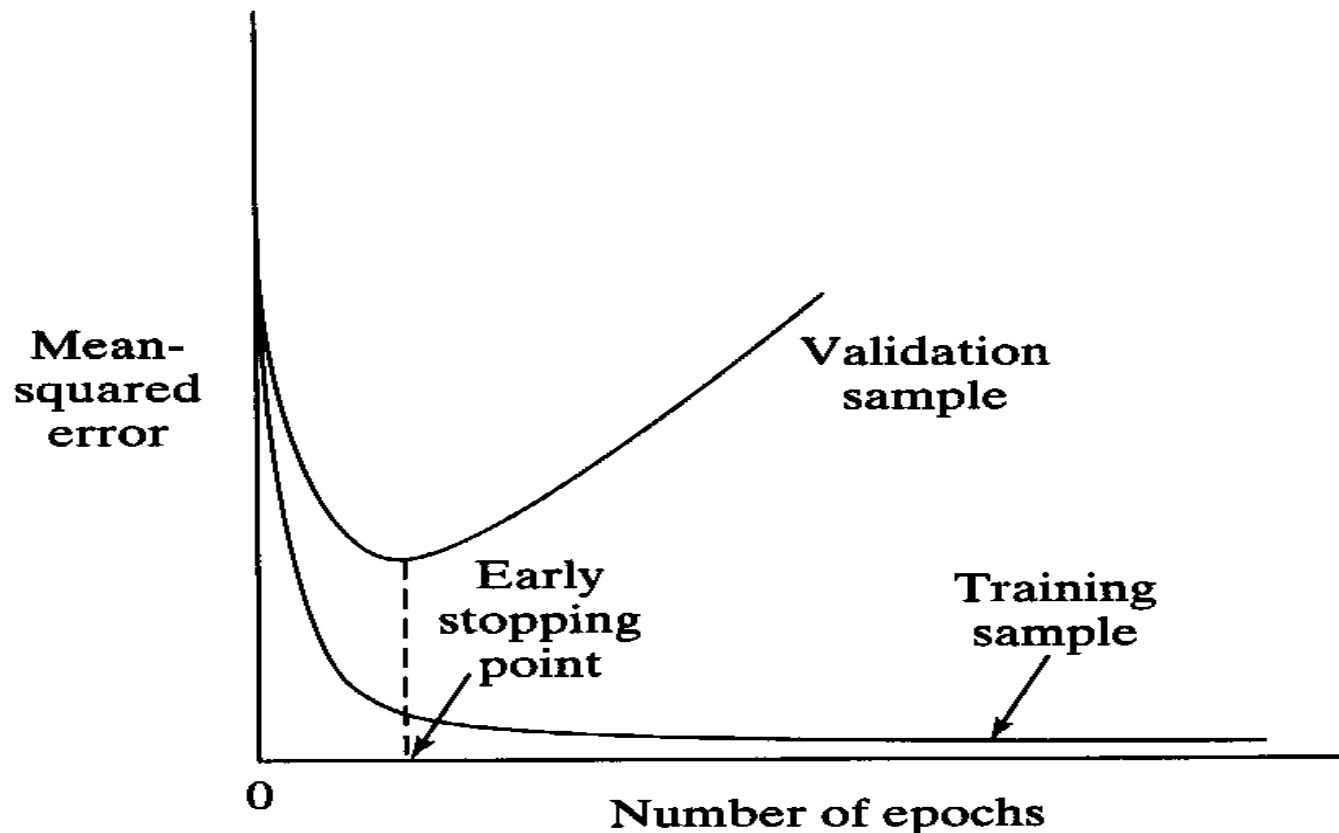
Properly fitted data  
(good generation)



Overfitted data  
(poor generation)

# Artificial Neural Networks

## Cross-Validation:



# Artificial Neural Networks

## NN Validation:

$$\text{Success Rate} = \frac{\text{Successfully identified samples}}{\text{Total validation samples}}$$

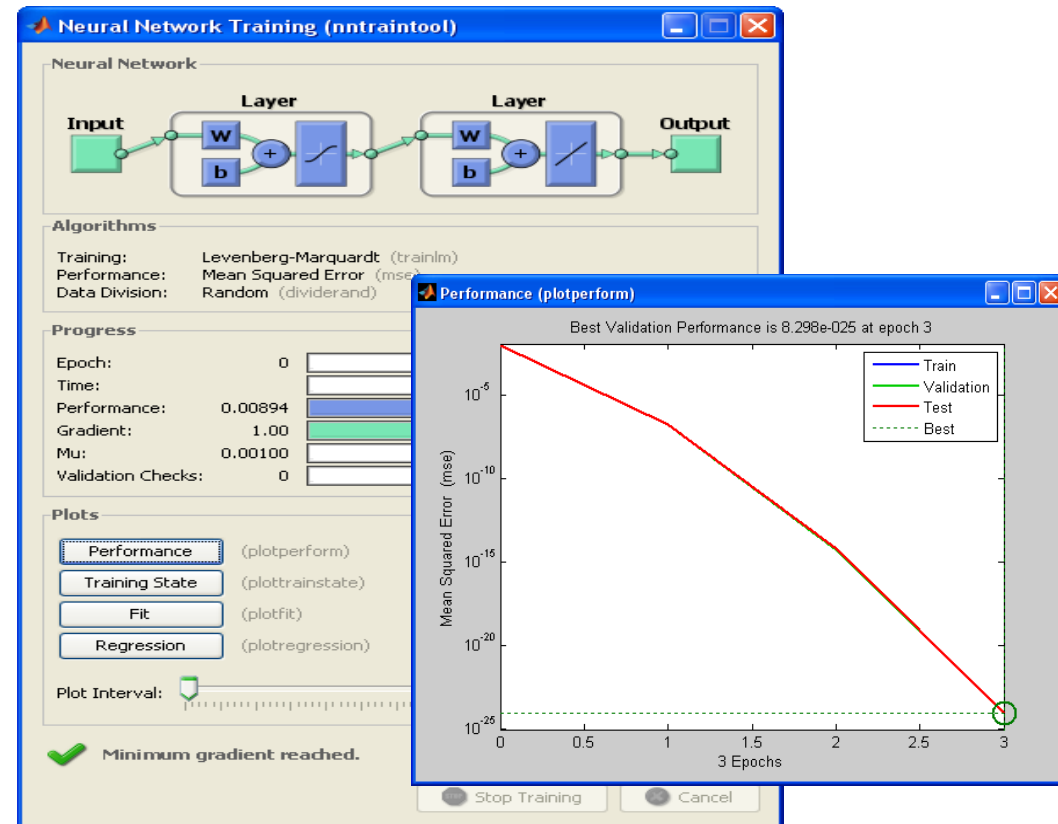
Confusion matrix:

		Actual Faults ==>		
		Fault 1	Fault 2	Fault 3
Predicted Faults <==	Fault 1	100%	0	0
	Fault 2	2%	98%	0
	Fault 3	0	0	100%

# Artificial Neural Networks

## Matlab Neural Network Toolbox - Design and simulate Neural Networks

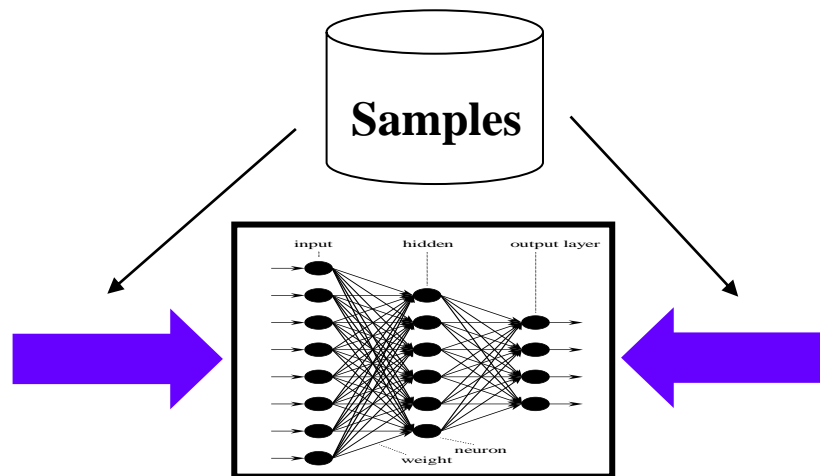
Neural Network Toolbox™  
provides tools for  
designing, implementing,  
visualizing, and simulating  
neural networks.



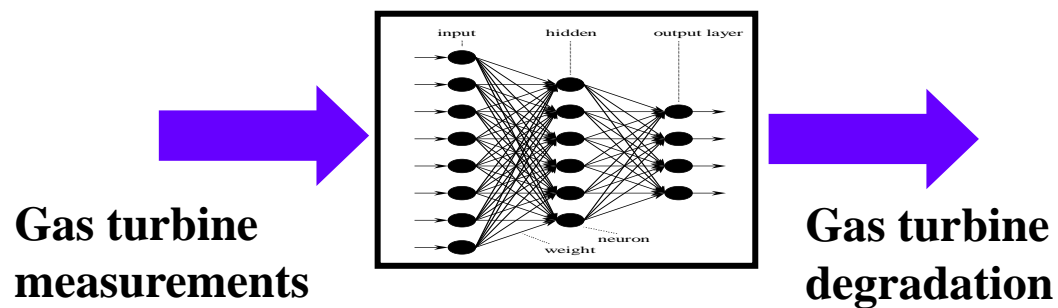


# Artificial Neural Networks

## Training of ANN:



## Application of ANN:



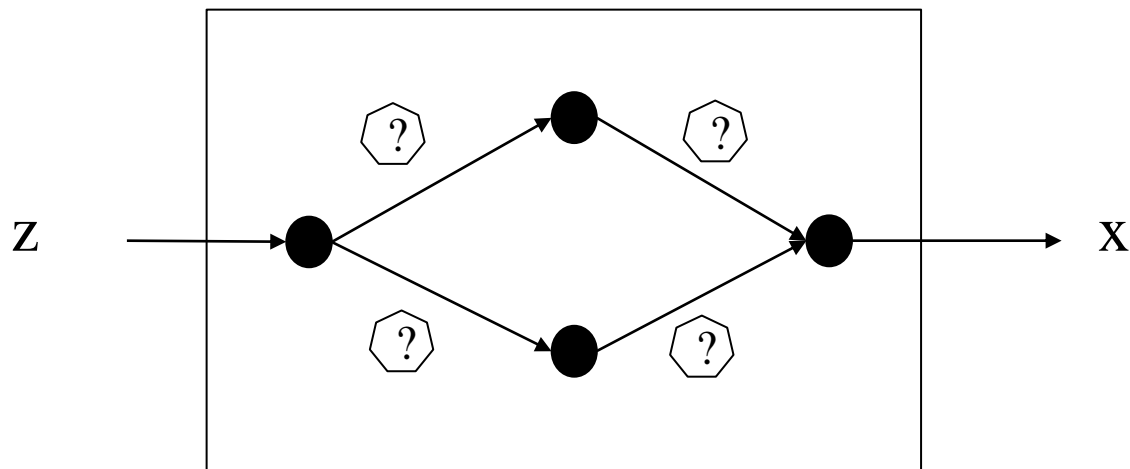
# *Artificial Neural Networks*

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## **Procedure of using a neural network:**

- ◆ **Choose a neural network configuration**
- ◆ **Generate samples** (experiments or simulations)
- ◆ **Split samples into training and testing/validation samples**
- ◆ **Training of neural network** (training samples)
- ◆ **Validation of neural network** (validation samples)
- ◆ **Application of neural network** (re-call mode)

# Simple Example



Two events (samples)

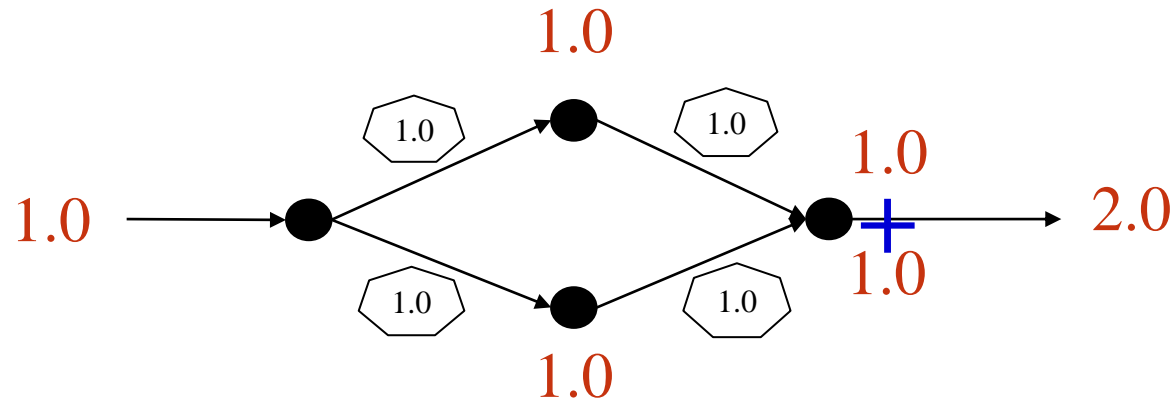
No.	(z, x)
1	(1.0, -1.0)
2	(-2.5, 2.5)

# Simple Example

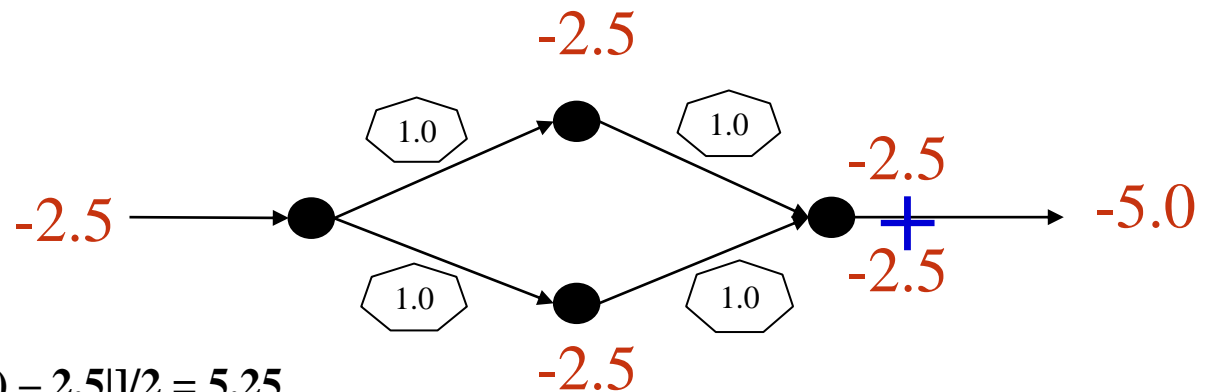
Assume all weights = 1 initially.

1<sup>st</sup> epoch:

1<sup>st</sup> sample (1.0, -1.0)



2<sup>nd</sup> sample (-2.5, 2.5)

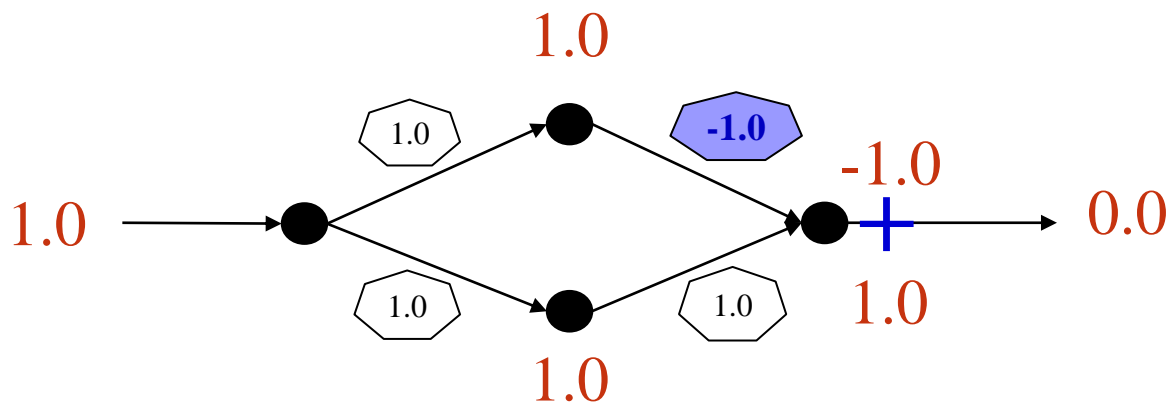


$$\text{Error} = [|(2) - (-1)| + |(-5) - 2.5|]/2 = 5.25$$

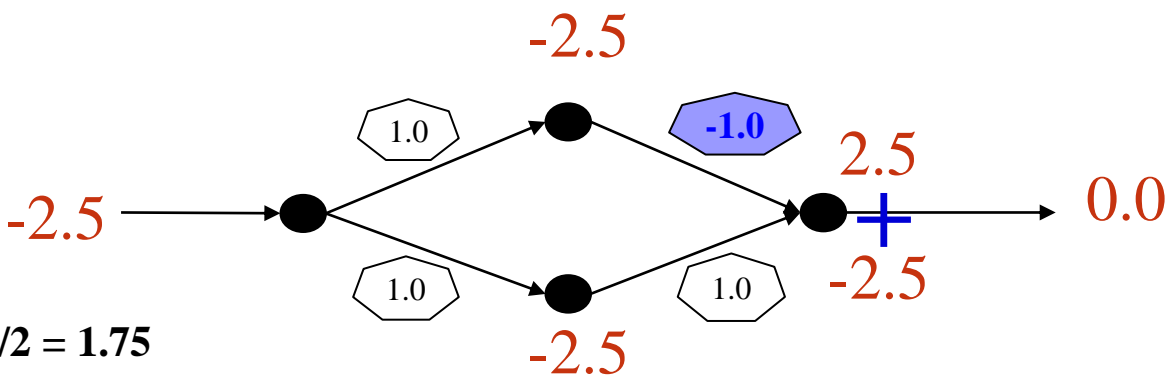
# Simple Example

2<sup>nd</sup> epoch:

1<sup>st</sup> sample (1.0, -1.0)



2<sup>nd</sup> sample (-2.5, 2.5):

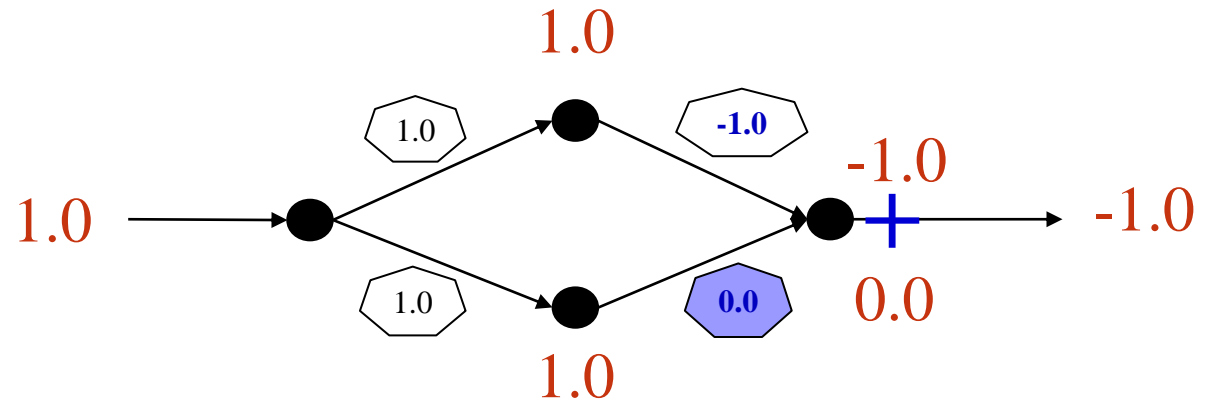


**Error =  $[|(0.0) - (-1.0)| + |0.0 - 2.5|]/2 = 1.75$**

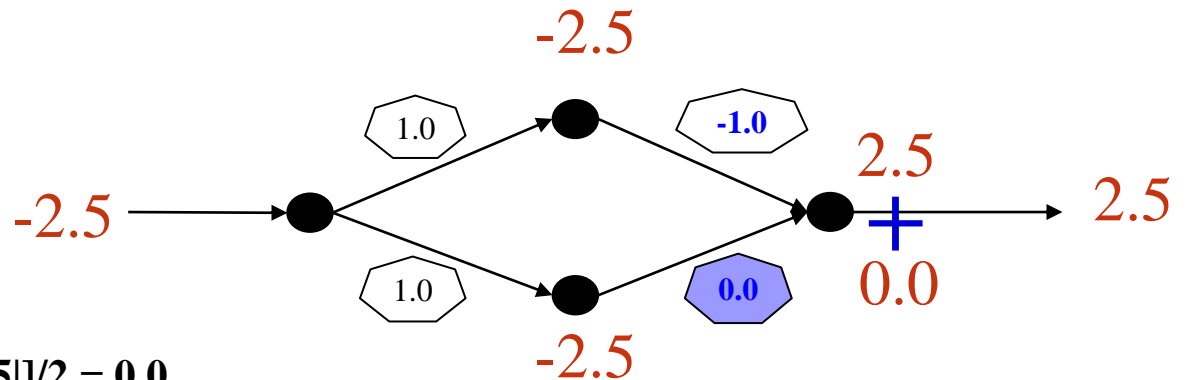
# Simple Example

3<sup>rd</sup> epoch:

1<sup>st</sup> sample (1.0, -1.0)

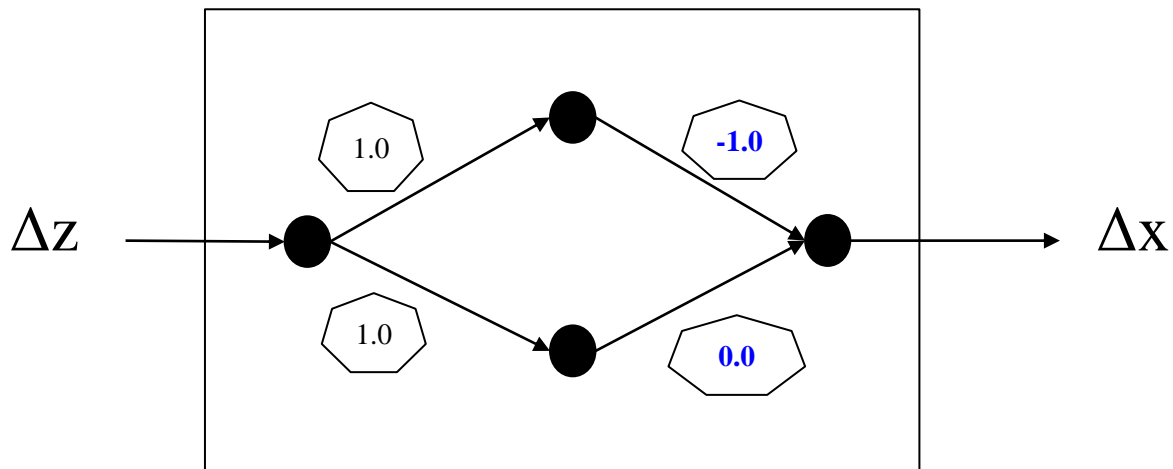


2<sup>nd</sup> sample (-2.5, 2.5):



$$\text{Error} = [ |(-1) - (-1)| + |2.5 - 2.5| ] / 2 = 0.0$$

# Simple Example

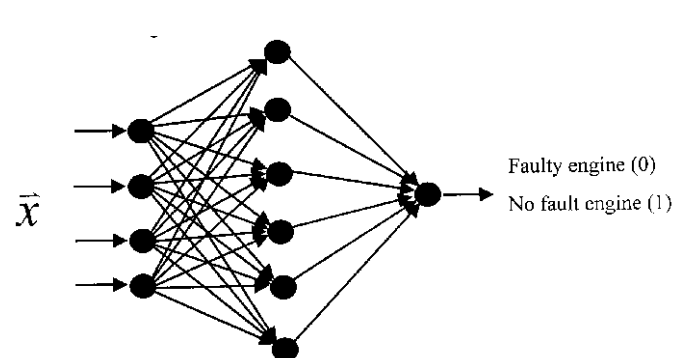


Two samples

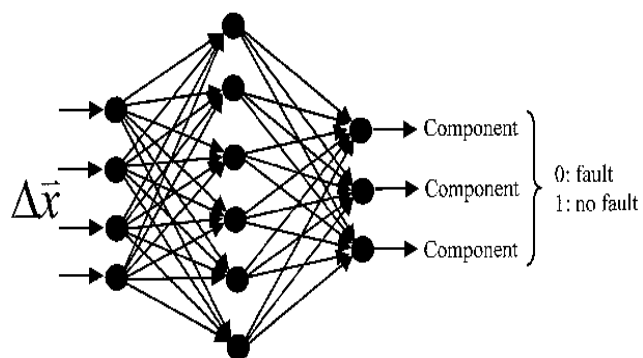
No.	$(\Delta z, \Delta x)$
1	(1.0, -1.0)
2	(-2.5, 2.5)

# Artificial Neural Networks

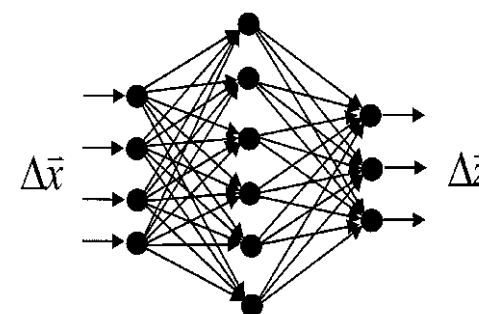
## Fault Detection



## Fault Isolation



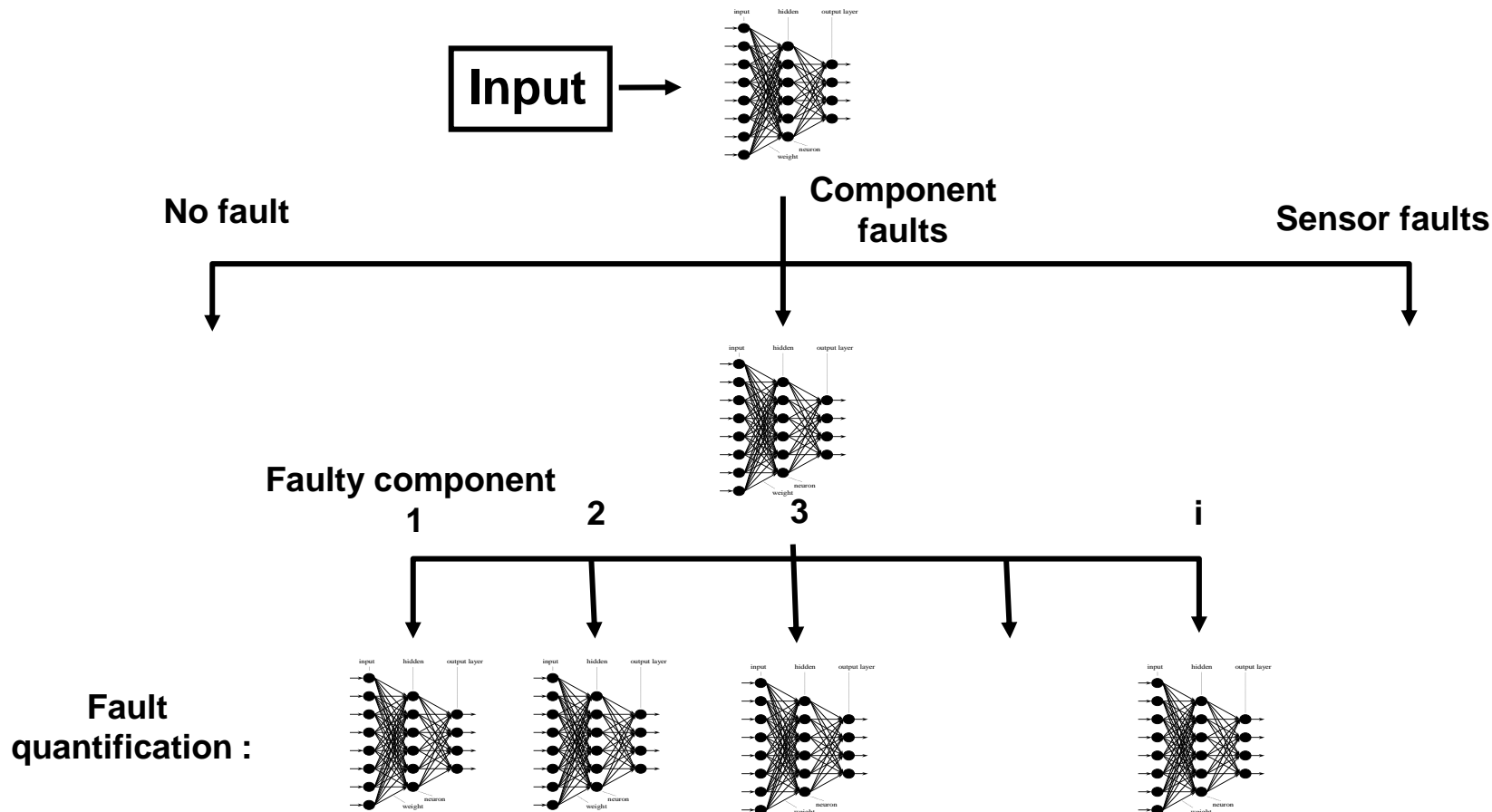
## Fault Quantification



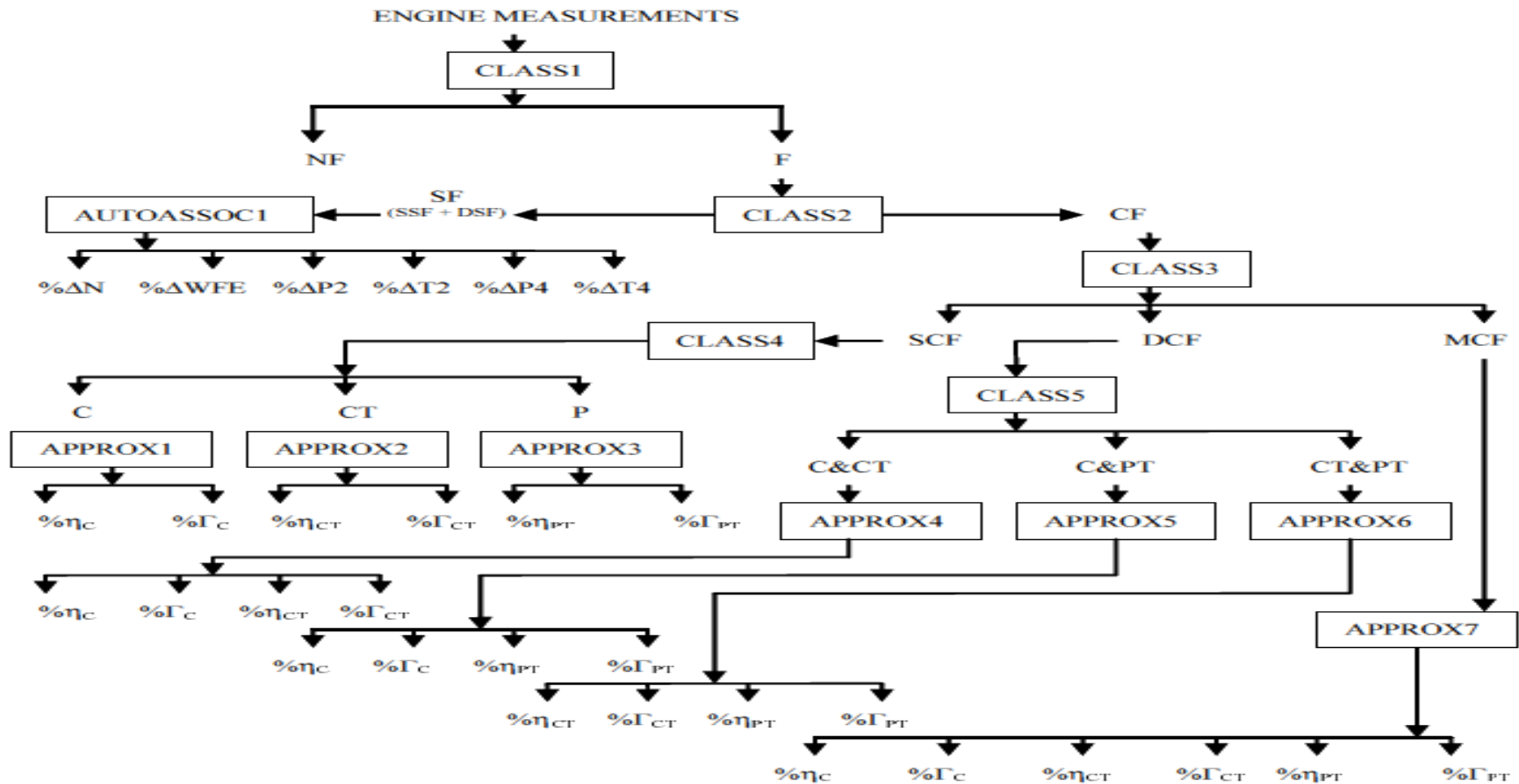


# Artificial Neural Networks

## A Neural Network Based Diagnostic system :



# Artificial Neural Networks



Gas turbine diagnostic framework for a single spool industrial gas turbine

# *Artificial Neural Networks*

---

## **Features :**

- ◆ Non-model based
- ◆ Very quick for application once trained – suitable for online or real time applications
- ◆ Accuracy can be very high
  
- ◆ Long time for training
- ◆ Large number of training & validation samples required
- ◆ Can only be used in training domain
- ◆ If the physical system is modified, the NNs should be trained again